



**European Commission
Research Programme of the Research Fund for Coal and Steel**

ANGELHY

**Innovative solutions for design and strengthening of
telecommunications and transmission lattice towers using large angles
from high strength steel and hybrid techniques of angles with
FRP strips**

WORK PACKAGE 5 – DELIVERABLE 5.1

Proposals for Code amendments

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1 Introduction

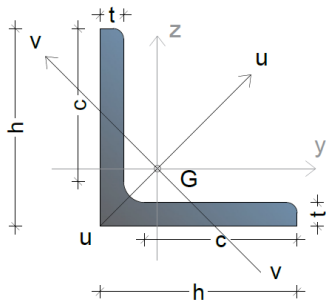
The code amendments for single angle and built-up members are presented in this deliverable through tables, and referred to prEN1993-1-1 [1], EN1993-1-5[2] and EN1993-3-1[3]. In the tables, there is a summary of the existing codes on the relevant topic as well as the proposal which came out from the investigations of ANGELHY project; the differences in the proposed formulas are distinguished with red colour from the existing ones.

More details of all the proposed formulas are available in Deliverable 4.4 [4] and Deliverable 3.4 [5], including examples of application.

2 Code amendments for single angle members

The code amendments for single angle members are summarized in the last column of Table 2.1.

Table 2.1: Code amendments for the design of single angle members

TOPIC	EXISTING RULES	ANGELHY PROPOSALS	CODE AMENDMENT
Classification system for equal leg angle cross-sections			
 <p> G centre of gravity h,t geometrical properties (c=h-t-r) u-u major principal axis or weak axis v-v minor principal axis or strong axis y,z geometrical axes </p>			
Part in compression Axial force N	<p><u>Class 3 limit</u></p> <p>1. limit prEN1993-1-1, Table 7.3, sheet 3: $\frac{h}{t} \leq 15\epsilon$ and $\frac{h}{t} \leq 11,5\epsilon$</p> <p>2. limit prEN1993-1-1, Table 7.3, sheet 2: $\frac{c}{t} \leq 14\epsilon$</p> <p>3. EN1993-1-5: $\frac{h}{t} \leq 13,9\epsilon$</p> <p>4. EN1993-3-1: $\frac{h}{t} \leq 15,9\epsilon$ or $\frac{h-2t}{t} \approx \frac{c}{t} \leq 13,9\epsilon$</p>	<p><u>Class 3 limit:</u> $\frac{c}{t} \leq 13,9\epsilon$ where c=h-t-r</p>	<p>prEN1993-1-1 (2019)</p> <p>§7.5 Classification of cross-sections</p> <p>Table 7.3 (sheet 3 of 3) should be modified properly, so as to cover the classifications of angle sections</p>

<p>Part in bending</p> <p>Strong axis bending M_u</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 10\epsilon$ (from prEN1993-1-1- Table 7.3, sheet 2)</p> <p><u>Class 3 limit:</u> $\frac{c}{t} \leq 14\epsilon$ (from prEN1993-1-1- Table 7.3, sheet 2)</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 16\epsilon$</p> <p><u>Class 3 limit:</u> $\frac{c}{t} \leq 26,3\epsilon$</p> <p>where $c=h-t-r$</p>	<p>prEN1993-1-1 (2019)</p> <p>§7.5 Classification of cross-sections</p> <p>Table 7.3 (sheet 3 of 3) should be modified properly, so as to cover the classifications of angle sections</p>
<p>Part in bending</p> <p>Weak axis bending M_v - tip in compression</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 16,6\epsilon$ (from prEN1993-1-1- Table 7.3, sheet 2, with $a_c=0,6$)</p> <p><u>Class 3 limit:</u> $\frac{c}{t} \leq 16\epsilon$ (from prEN1993-1-1- Table 7.3, sheet 2, with $K_\sigma=0,57$)</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 14\epsilon$</p> <p><u>Class 3 limit:</u> $\frac{c}{t} \leq 26,9\epsilon$</p> <p>where $c=h-t-r$</p>	<p>prEN1993-1-1 (2019)</p> <p>§7.5 Classification of cross-sections</p> <p>Table 7.3 (sheet 3 of 3) should be modified properly, so as to cover the classifications of angle sections</p>
<p>Part in bending</p> <p>Weak axis bending M_v -tip in tension</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 40\epsilon$ (from prEN1993-1-1- Table 7.3, sheet 2, with $a_c=0,4$)</p>	<p><u>Class 2 limit:</u> $\frac{c}{t} \leq 30\epsilon$</p> <p>where $c=h-t-r$</p>	<p>prEN1993-1-1 (2019)</p> <p>§7.5 Classification of cross-sections</p> <p>Table 7.3 (sheet 3 of 3) should be modified properly, so as to cover the classifications of angle sections</p>
<p>Cross-section characteristic resistance for equal leg angles</p>			
<p>Compression axial force N</p> <p>EN1993-1-1 & EN1993-3-1 combined with EN1993-1-5</p>	<p>Design resistance - class 1,2,3:</p> $N_{Rk} = \frac{A f_y}{\gamma_{M0}}$ <p>Design resistance - class 4:</p> $N_{Rk} = \frac{A_{eff} f_y}{\gamma_{M0}}$ <p>where:</p> $A_{eff} = A - 2ct(1 - \rho)$ $\bar{\lambda}_p = \frac{\bar{b}/t}{18,6\epsilon}$ <p>EN 1993-1-5 defines $\bar{b} = h$</p> <p>EN 1993-3-1 defines $\bar{b} = h-2t$</p> <p>- $\rho = 1$, for $\bar{\lambda}_p \leq 0,748$</p> <p>- $\rho = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$</p>	<p>Design resistance - class 1,2,3: $N_{c,Rk} = \frac{A f_y}{\gamma_{M0}}$</p> <p>Design resistance - class 4: $N_{c,Rk} = \frac{A_{eff} f_y}{\gamma_{M0}}$</p> <p>where: $A_{eff} = A - 2ct(1 - \rho)$</p> $\bar{\lambda}_p = \frac{c/t}{18,6\epsilon}$ <p>where $c=h-t-r$</p> <p>- $\rho = 1$, for $\bar{\lambda}_p \leq 0,748$</p> <p>- $\rho = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$</p>	<p>EN1993-1-5</p> <p>In §4.4 (2), $\bar{b} = h$ should be replaced by $\bar{b} = c$ for equal leg angle profiles</p>

<p>Strong axis bending M_u</p> <p>prEN1993-1-1</p>	<p>Design resistance:</p> $M_{u,Rk} = W_u \frac{f_y}{\gamma_{M0}}$ <p>where,</p> <p>$W_u = W_{pl,u}$ for class 1 or 2</p> <p>$W_u = W_{el,u}$ for class 3</p> <p>$W_u = W_{eff,u}$ for class 4</p>	<p>Design resistance: $M_{u,Rk} = W_u \frac{f_y}{\gamma_{M0}}$</p> <p>Where $W_u = \alpha_{i,u} W_{el,u}$, $i = 2, 3, 4$</p> <p>$\alpha_{2,u} = 1,5$ for class 1 or 2</p> <p>$\alpha_{3,u} = \left[1 + \left(\frac{26,3\varepsilon - c/t}{26,3\varepsilon - 16\varepsilon} \right) \cdot (1,5 - 1) \right]$ for class 3</p> <p>$\alpha_{4,u} = W_{eff,u} / W_{el,u} = \rho_u^2$ for class 4</p> $\bar{\lambda}_p = \frac{c/t}{35,58\varepsilon}$ <p>- $\rho_u = 1$, for $\bar{\lambda}_p \leq 0,748$</p> <p>- $\rho_u = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$</p>	<p>prEN1993-1-1 (2019)</p> <p>§8.2.2.6 Section properties for the characteristic resistances</p> <p>Table 8.1 should be modified properly, so as to include the properties for angle sections</p> <p>----</p> <p>EN1993-1-5</p> <p>In §4.4, Table 4.2 $K\sigma$ factors for fix-free boundary conditions should be added</p>
<p>Weak axis bending M_v tip in compression</p> <p>prEN1993-1-1</p>	<p>Design resistance:</p> $M_{v,Rk} = W_v \frac{f_y}{\gamma_{M0}}$ <p>where,</p> <p>$W_v = W_{pl,v}$ for class 1 or 2</p> <p>$W_v = W_{el,v}$ for class 3</p> <p>$W_v = W_{eff,v}$ for class 4</p>	<p>Design resistance: $M_{v,Rk} = W_v \frac{f_y}{\gamma_{M0}}$</p> <p>Where $W_v = \alpha_{i,v} W_{el,v}$, $i = 2, 3, 4$</p> <p>$\alpha_{2,v} = W_{pl,v} / W_{el,v}$ for class 1 or 2</p> <p>$\alpha_{3,v} = \left[1 + \left(\frac{26,9\varepsilon - c/t}{26,9\varepsilon - 14\varepsilon} \right) \cdot \left(\frac{W_{pl,v}}{W_{el,v}} - 1 \right) \right]$ for class 3</p> <p>$\alpha_{4,v} = W_{eff,v} / W_{el,v} = 0,94 \cdot \rho_v^2$ for class 4</p> $\bar{\lambda}_p = \frac{c/t}{36,48\varepsilon}$ <p>- $\rho_v = 1$, for $\bar{\lambda}_p \leq 0,748$</p> <p>- $\rho_v = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$</p>	<p>prEN1993-1-1 (2019)</p> <p>§8.2.2.6 Section properties for the characteristic resistances</p> <p>Table 8.1 should be modified properly, so as to include the properties for angle sections</p> <p>----</p> <p>EN1993-1-5</p> <p>In §4.4, Table 4.2 $K\sigma$ factors for fix-free boundary conditions should be added</p>
<p>Weak axis bending M_v tip in tension</p> <p>prEN1993-1-1</p>	<p>Design resistance:</p> $M_{v,Rk} = W_v \frac{f_y}{\gamma_{M0}}$ <p>where,</p> <p>$W_v = W_{pl,v}$ for class 1 or 2</p> <p>$W_v = W_{el,v}$ for class 3</p> <p>$W_v = W_{eff,v}$ for class 4</p>	<p>Design resistance:</p> $M_{v,Rk} = W_{pl,v} \frac{f_y}{\gamma_{M0}}$	<p>prEN1993-1-1 (2019)</p> <p>§8.2.2.6 Section properties for the characteristic resistances</p> <p>Table 8.1 should be modified properly, so as to include the properties for angle sections</p>

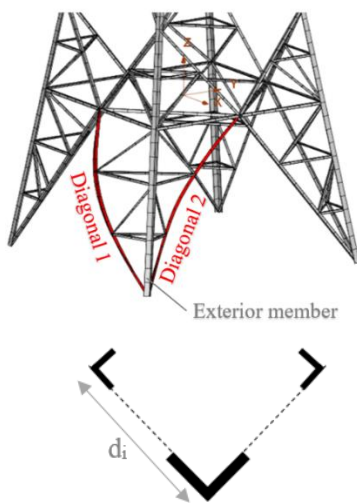
Member resistance - Stability for equal leg angles			
<p>Axial force N prEN1993-1-1</p>	<p>prEN1993-1-1 (2019): §8.3.1 Uniform members in compression</p> <p>Curve b or a are used, based on steel grade according to prEN1993-1-1 (2019)</p> <p>Using of relevant buckling mode for the evaluation of the non-dimensional slenderness</p>	<p>Design resistance - class 1,2,3:</p> $N_{b,Rd} = \frac{\chi_{min} A f_y}{\gamma_{M1}}$ <p>where: $\chi_{min} = \min\{\chi_u, \chi_v\}$</p> $\bar{\lambda}_u = \sqrt{\frac{A f_y}{N_{cr,u}}}, \quad \bar{\lambda}_v = \sqrt{\frac{A f_y}{N_{cr,v}}}$ <p>χ_u, χ_v derived from buckling curves a and b (prEN1993-1-1:2019)</p> <p>Design resistance - class 4:</p> $N_{Rd} = \frac{\chi_{min} A_{eff} f_y}{\gamma_{M1}}$ <p>where: $\chi_{min} = \min\{\chi_u, \chi_v\}$</p> <p>$\chi_u, \chi_v$ derived from buckling curves a and b (prEN1993-1-1:2019) as for class 1 to 3</p> <p>cross-sections</p> $A_{eff} = A - 2ct(1 - \rho)$ $\bar{\lambda}_p = \sqrt{\chi_{min} \frac{c/t}{18,6\varepsilon}}$ <p>where $c=h-t-r$</p> <ul style="list-style-type: none"> - $\rho = 1$, for $\bar{\lambda}_p \leq 0,748$ - $\rho = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$ 	<p>prEN1993-1-1 (2019) §8.3.1.2 Slenderness of compression members</p> <p>A sub-paragraph should be added for angle cross-sections to use $\bar{\lambda}_b = \{\bar{\lambda}_u; \bar{\lambda}_v\}$</p>
<p>Strong axis bending M_u prEN1993-1-1</p>	<p>prEN1993-1-1 (2019): §8.3.2 Uniform members in bending</p> <p>Curve d is used</p>	<p>Design resistance: $M_{u,Rd} = \chi_{LT} W_u \frac{f_y}{\gamma_{M1}}$</p> <p>where: $\bar{\lambda}_{LT} = \sqrt{\frac{W_u f_y}{M_{cr}}}$</p> <p>$\chi_{LT}$ as function of the LTB slenderness derived from buckling curve a. Buckling curve is given from the equations</p> $\chi_{LT} = \frac{1}{\Phi_{LT} + \sqrt{\Phi_{LT}^2 - \bar{\lambda}_{LT}^2}}$ <p>but $\begin{cases} \chi_{LT} \leq 1,0 \\ \chi_{LT} \leq 1/\bar{\lambda}_{LT}^2 \end{cases}$</p> $\Phi_{LT} = 0,5[1 + \alpha_{LT}(\bar{\lambda}_{LT} - 0,4) + \bar{\lambda}_{LT}^2]$ <p>LTB may be ignored and $\chi_{LT} = 1,0$ when one of the following conditions apply:</p> <ul style="list-style-type: none"> • $\bar{\lambda}_{LT} \leq \bar{\lambda}_{LT,0}$ with $\bar{\lambda}_{LT,0} = 0,4$ • $\frac{M_{Ed}}{M_{cr}} \leq \bar{\lambda}_{LT,0}^2$ 	<p>prEN1993-1-1 (2019) §8.3.2.3 Buckling reduction factors χ_{LT} for lateral torsional buckling</p> <p>In Table 8.4, the proposed buckling curve d for angles should be changed to a.</p> <p>A sub-paragraph should be added for the definition of the buckling curves (with doubling the plateau)</p>

		<ul style="list-style-type: none"> • $\frac{N_{Ed}}{N_{bu,Rd}} > 0,5$ • $\frac{N_{Ed}}{N_{bv,Rd}} > 0,5$ <p>Critical LTB moment: $M_{cr} = C_b \frac{0,46 \cdot E \cdot I^2 \cdot t^2}{l}$</p> $C_b = \frac{12,5 M_{max}}{2,5 M_{max} + 3 M_A + 4 M_B + 3 M_C} \leq 1,5$ <p>For linear moment distribution with -1</p> $\leq \psi = \frac{M_2}{M_1} \leq 1, \quad C_b = \frac{12,5}{7,5 + 5\psi}$ $W_u = \alpha_{i,u} W_{el,u}, \quad i = 2, 3, 4$ $\alpha_{2,u} = 1,5 \quad \text{for class 1 or 2}$ $\alpha_{3,u} = \left[1 + \left(\frac{26,3\varepsilon - c/t}{26,3\varepsilon - 16\varepsilon} \right) \cdot (1,5 - 1) \right] \quad \text{for class 3}$ $\alpha_{4,u} = W_{eff,u} / W_{el,u} = \rho_u^2 \quad \text{for class 4}$ $\bar{\lambda}_p = \sqrt{\chi_{LT}} \frac{c/t}{35,58\varepsilon}$ <ul style="list-style-type: none"> - $\rho_u = 1$, for $\bar{\lambda}_p \leq 0,748$ - $\rho_u = \frac{\bar{\lambda}_p^{-0,188}}{\bar{\lambda}_p^2}$, for $\bar{\lambda}_p > 0,748$ 	
Weak axis bending M_v prEN1993-1-1	Same with the cross-section resistance, independent of the member length	Same with the cross-section resistance, independent of the member length	Same as above
$N+M_u+M_v$ prEN1993-1-1	prEN1993-1-1 (2019): §8.3.3 Uniform members in bending and axial compression $\frac{N_{Ed}}{\chi_y N_{Rk}} + k_{yy} \frac{M_{y,Ed} + \Delta M_{y,Ed}}{\chi_{LT} \frac{M_{y,Rk}}{\gamma_{M1}}} + k_{yz}$ $\frac{N_{Ed}}{\chi_z N_{Rk}} + k_{zy} \frac{M_{y,Ed} + \Delta M_{y,Ed}}{\chi_{LT} \frac{M_{y,Rk}}{\gamma_{M1}}} + k_{zz}$	$\left(\frac{N_{Ed}}{N_{Rd}} + k_{uu} \frac{M_{u,Ed}}{M_{u,Rd}} \right)^\xi + k_{uv} \frac{M_{v,Ed}}{M_{v,Rd}} \leq 1$ $\left(\frac{N_{Ed}}{N_{Rd}} + k_{vu} \frac{M_{u,Ed}}{M_{u,Rd}} \right)^\xi + k_{vv} \frac{M_{v,Ed}}{M_{v,Rd}} \leq 1$ $k_{uu} = \frac{C_u}{1 - \frac{N_{Ed}}{N_{cr,u}}}; \quad k_{uv} = C_v; \quad k_{vu} = C_u$ $; \quad k_{vv} = \frac{C_v}{1 - \frac{N_{Ed}}{N_{cr,v}}}$ $C_u = 0,6 + 0,4\psi_u; \quad -1 \leq \psi_u = \frac{M_{2u}}{M_{1u}} \leq 1$ $C_v = 0,6 + 0,4\psi_v; \quad -1 \leq \psi_v = \frac{M_{2v}}{M_{1v}} \leq 1$ <p>Interaction factor ξ:</p> $c/t \leq 16\varepsilon: \quad \xi = 2$ $16\varepsilon < c/t < 26,3\varepsilon:$ $\xi = \left[1 + \left(\frac{26,3\varepsilon - c/t}{26,3\varepsilon - 16\varepsilon} \right) \cdot (2 - 1) \right]$ $c/t > 26,3\varepsilon: \quad \xi = 1$	prEN1993-1-1 (2019) §8.3.3 Uniform members in bending and axial compression A sub-paragraph should be added for equal leg angle profiles

<p>General method prEN1993-1-1</p>	<p>prEN1993-1-1 (2019): §8.3.4 General method for lateral and lateral torsional buckling of structural components</p> $\chi_{op} \cdot a_{ult,k} \geq 1,0$ $\chi_{op} = \min \{ \chi_b; \chi_{LT} \}$ $\alpha_{ult,k} = \frac{\sigma_{max}}{f_y} = \frac{\sigma_N}{f_y} + \frac{\sigma_{e_0}}{f_y} +$ $\bar{\lambda}_{op} = \sqrt{\frac{\alpha_{ult,k}}{\alpha_{cr,op}}}$	$\chi_{op} \cdot a_{ult,k} \geq 1,0$ $\chi_{op} = \min \{ \chi_u; \chi_v \}$ $\alpha_{ult,k} = \frac{\sigma_{max}}{f_y} = \frac{\sigma_N}{f_y} + \frac{\sigma_{e_0}}{f_y} + \frac{\sigma_M}{f_y}$ $\bar{\lambda}_{op} = \sqrt{\frac{\alpha_{ult,k}}{\alpha_{cr,op}}}$ <p>Where $\alpha_{cr,op}$ is the minimum load amplifier for the design loads to reach the elastic critical load of the structural component associated to weak axis buckling.</p>	<p>prEN1993-1-1 (2019) §8.3.4 General method for lateral and lateral torsional buckling of structural components</p> <p>A sub-paragraph should be added with clarifications of the use of general method for equal leg angle profiles</p>
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Segment instability of lattice towers

<p>Segment instability of pylons</p>	<p>This mode of instability is not covered by the current codes</p>	<p><u>Two models are proposed:</u></p> <p><u>Simplified model:</u> $a_{cr} = \frac{2\pi^2 E I_y}{L^2 \cdot (P_1 + P_2)}$</p> <p><u>Final model:</u> $a_{cr} = \frac{N_{cr}}{P_1 + P_2}$</p> $N_{cr} = \frac{\pi^2 E I_{y,tot}}{L^2} + \frac{3}{16} K_T L$ $K_T = \frac{4}{m^2} (2R_{mean})$ $R_{mean} = \frac{3C}{2L_{ext}} \cdot \frac{1}{n} \sum_{i=1}^n \frac{1}{d_i^2}$ <p>The <u>ultimate resistance</u> in both cases is</p> $\frac{1}{a_u} = \frac{1}{a_{cr}} + \frac{0,96}{a_{pl}}$	<p>EN1993-3-1 §6.3.1 Resistance of members-compression members</p> <p>A sub-paragraph should be added, indicated to check the possible appearance of a segment instability.</p> <p>An Annex should be added, covering the calculations of the segment instability</p>
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α_{cr} is the critical load multiplier;

α_{pl} is the plastic load multiplier equals $\alpha_{pl} = \frac{2 \cdot N_{pl}}{P_1 + P_2}$;

N_{pl} is the plastic resistance of the diagonal's cross-section ($N_{pl} = A f_y$);

α_u is the ultimate load multiplier;

I_y is the moment of inertia about y-y geometrical axis of the diagonal's cross-section;

L is the buckling length of the diagonal;

E is the modulus of elasticity;

P_1, P_2 are the axial forces in the two diagonals;

$I_{y,tot}$ is the total moment of inertia about y-y geometrical axis of both diagonals (i.e $I_{y,tot} = 2I_y$);

m is the number of zones of length of the leg $l_i = L/m$ separated by rigid horizontal triangles in the leg; the accuracy of the formulae for K_T is sufficient for a value of $m \leq 6$ (i.e for maximum 5 horizontal rigid triangles in the leg).

C is the torsional rigidity of the cross-section;

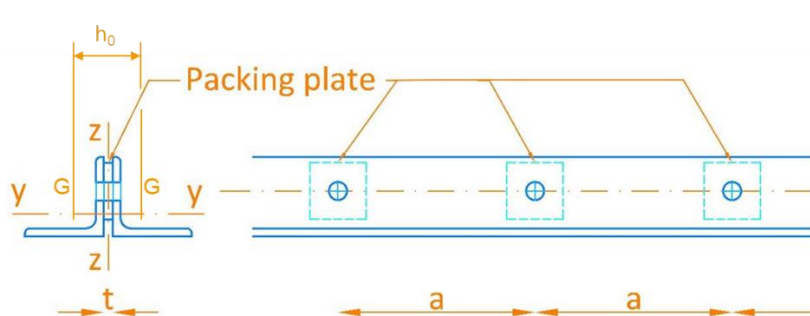
L_{ext} is the length of the exterior (main) member of the leg;

	<p>d_i is the horizontal distance of the longitudinal axis of the diagonal from the longitudinal axis of the main leg, at the i horizontal level.</p>
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3 Code amendments for built-up members

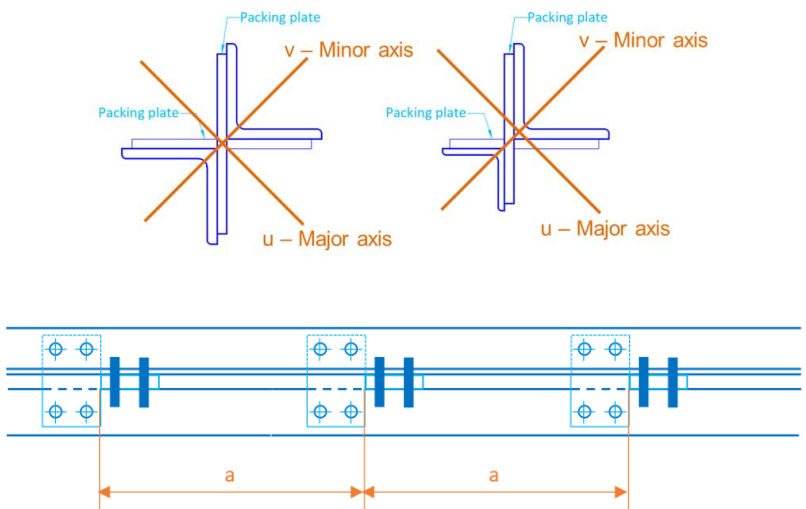
Table 3.1 summarizes the ANGELHY proposals for the design of built-up members. These modifications might be introduced into section 8.4.5 of prEN 1993-1-1 in order to propose a design model.

Table 3.1: Code amendments for the design of closely spaced built-up sections

TOPIC	EXISTING RULES	ANGELHY PROPOSALS	CODE AMENDMENT
Buckling resistance of back to back connected angle section members			
			
<p> $z-z$: Major axis $y-y$: Minor axis h_0: Distance between the centroids a: Distance between the packing plates i_v: Radius of gyration about the angle section's minor axis (see Table 2.1) L: Member length i_z: Radius of gyration of the built-up section member considered as integral about $z-z$ </p>			
Major axis buckling	<p><u>prEN1993-1-1 (2019):</u> If $a \leq 15i_v$: Member may be treated as integral without considering the influence of the connections. Buckling resistance is determined based on:</p> <ul style="list-style-type: none"> Reduction curve b – steel grades up to S420 Reduction curve a – for higher steel grades up to S700 <p><u>If $a > 15i_v$:</u> The influence of connections and the resulting shear stiffness should be accounted for. No design proposal is provided.</p> <p><u>EN 50341-1 (2015)</u> Independently from the packing plate distance, the buckling</p>	<p><u>Buckling resistance:</u></p> $\frac{N_{Ed}}{\chi \frac{A f_y}{\gamma_{M1}}} \leq 1,0$ <p>χ: is the buckling reduction factor determined based on the slenderness $\bar{\lambda}_{sv}$ and buckling curve b</p> $\bar{\lambda}_{sv} = \sqrt{\frac{A f_y}{N_{cr,sv}}}$ <p>The critical axial force $N_{cr,sv}$ considering the influence of the shear stiffness is calculated as follows:</p> $N_{cr,sv} = \frac{1}{\frac{1}{N_{cr}} + \frac{1}{S_v}}$	<p>prEN1993-1-1 (2019)</p> <p>§8.4.5 Closely spaced-built up members</p>

	<p>resistance is based the effective geometric slenderness λ_{zi}:</p> $\lambda_{zi} = \sqrt{\lambda_z^2 + \lambda_1^2 \frac{m}{2}}$ <p>λ_z: geometric slenderness of the built-up member considered as uniform - $\lambda_z = L/i_z$</p> <p>λ_1: geometric slenderness of an individual angle section between packing plates - $\lambda_1 = a/i_v$</p> <p>m: number of angle sections</p>	<p>N_{cr}: is the critical axial force of the built-up member considered as integral neglecting the influence of the shear stiffness</p> <p>S_v: is the shear stiffness of the built-up member determined depending on the connection type as follows:</p> <p><u>For members connected through fit bolts:</u></p> $S_v = S_{v1} = \frac{1}{\frac{a^2}{24EI_{v,ch}}}$ <p>$I_{v,ch}$: is the 2nd moment of area of one angle section about its minor axis</p> <p><u>For members connected preloaded bolts:</u></p> $S_v = S_{v2} = \frac{1}{\frac{a^2}{24EI_{v,ch}} + \frac{ah_0}{12EI_{pp}}}$ <p>I_{pp}: is the 2nd moment of area of the effective part of the packing plate</p> $I_{pp} = \frac{\pi(B + 2t + t_p)^4 - \pi d^4}{64}$ <p>t: is the thickness of the angle section t_p: is the thickness of the packing plate B: is the inside diameter of the bolt head (noted s in EN 14399) d: is the diameter of the hole</p> <p>S_{v2} may also be applied if the design slip resistance $F_{s,Rd}$ for non fully preloaded bolt connections is higher than the shear force to be transmitted.</p> <p><u>Connection resistance:</u> The resistance of the connection should be verified according to EN 1993-1-8 based on the shear force V_{Ed} calculated as follows:</p> $V_{Ed} = \frac{\pi a}{L h_0} M_{Ed}$ $M_{Ed} = \frac{N_{Ed} \frac{L}{200}}{1 - \frac{N_{Ed}}{N_{cr,SV}}}$	
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Resistance of star batted back to back connected angle section members



- v-v : Major axis
- u-u : Minor axis
- h₀: Distance between the centroids of the angle sections
- a: Distance between the packing plates
- i_v: Radius of gyration about the angle section's minor axis (see Table 2.1)
- L: Member length
- i_z: Radius of gyration of the built-up section member considered as integral about z-z

Flexural buckling	<p><u>prEN1993-1-1 (2019):</u> If $a \leq 70i_v$: Member may be treated as integral without considering the influence of the connections. Buckling resistance is determined based on:</p> <ul style="list-style-type: none"> • Reduction curve b – steel grades up to S420 • Reduction curve a – for higher steel grades up to S700 <p style="text-align: center;"><u>If $a > 70i_v$:</u> The influence of connections and the resulting shear stiffness should be accounted for. No design proposal is provided.</p> <p style="text-align: center;"><u>EN 50341-1 (2015)</u> Independently from the packing plate distance, the buckling resistance is based the effective geometric slenderness λ_{zi}:</p> $\lambda_{zi} = \sqrt{\lambda_z^2 + \lambda_1^2 \frac{m}{2}}$ <p>λ_z: geometric slenderness of the built-up member considered as uniform - $\lambda_z = L/i_z$</p>	<p style="text-align: center;"><u>Buckling resistance:</u></p> <p>The buckling resistance should be checked about both principle axis. For simplicity the index indicating the relevant axis is omitted in the following.</p> $\chi \frac{N_{Ed}}{A f_y} \leq 1,0$ <p>χ: is the buckling reduction factor determined based on the slenderness $\bar{\lambda}_{sv}$ and buckling curve <i>b</i></p> $\bar{\lambda}_{sv} = \sqrt{\frac{A f_y}{N_{cr,sv}}}$ <p>The critical axial force $N_{cr,sv}$ considering the influence of the shear stiffness is calculated as follows:</p> $N_{cr,sv} = \frac{1}{\frac{1}{N_{cr}} + \frac{1}{S_v}}$ <p>N_{cr}: is the critical axial force of the built-up member considered as integral neglecting the influence of the shear stiffness</p> <p>S_v: is the shear stiffness of the built-up member determined depending on the connection type as follows:</p>	<p>prEN1993-1-1 (2019) §8.4.5 Closely spaced-built up members</p>
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	<p>λ_1: geometric slenderness of an individual angle section between packing plates - $\lambda_1 = a/i_v$</p> <p>m: number of angle sections</p>	<p><u>For members connected through fit bolts:</u></p> $S_v = S_{v1} = \frac{1}{24EI_{v,ch} a^2}$ <p>$I_{v,ch}$: is the 2nd moment of area of one angle section about its minor axis</p> <p><u>For members connected preloaded bolts:</u></p> $S_v = S_{v2} = \frac{1}{\frac{a^2}{24EI_{v,ch}} + \frac{ah_0}{12EI_{pp}}}$ <p>I_{pp}: is the 2nd moment of area of the effective part of the packing plate</p> $I_{pp} = \frac{\pi(B + 2t + t_p)^4 - \pi d^4}{32}$ <p>t: is the thickness of the angle section t_p: is the thickness of the packing plate B: is the inside diameter of the bolt head (noted s in EN 14399) d: is the diameter of the hole</p> <p>S_{v2} may also be applied if the design slip resistance $F_{s,Rd}$ for non fully preloaded bolt connections is higher than the shear force to be transmitted.</p> <p><u>Connection resistance:</u> The resistance of the connection should be verified according to EN 1993-1-8 based on the shear force V_{Ed} calculated as follows:</p> $V_{Ed} = \frac{1}{2} \frac{\pi a}{L h_0} M_{Ed}$ $M_{Ed} = \frac{N_{Ed} \frac{L}{200}}{1 - \frac{N_{Ed}}{N_{cr,SV}}}$	
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<p>Interaction between axial force and bending</p>	<p>prEN1993-1-1 (2019): No suitable design method is provided</p> <p>Elastic 2nd order analysis is the only option but the imperfection amplitude is not well defined</p>	<p style="text-align: center;"><u>Interaction equations:</u></p> <p>The following interaction equations may be applied if at least two intermediate pairs of batten plates are used along the built-up member.</p> $\left(\frac{N_{Ed}}{\chi_u \frac{N_{Rk}}{\gamma_{M1}}} + k_{uu} \frac{M_{u,Ed}}{\chi_{LT} \frac{M_{u,Rk}}{\gamma_{M1}}} \right)^\xi + k_{uv} \frac{M_{v,Ed}}{\frac{M_{v,Rk}}{\gamma_{M1}}} \leq 1$ $\left(\frac{N_{Ed}}{\chi_v \frac{N_{Rk}}{\gamma_{M1}}} + k_{vu} \frac{M_{u,Ed}}{\chi_{LT} \frac{M_{u,Rk}}{\gamma_{M1}}} \right)^\xi + k_{vv} \frac{M_{v,Ed}}{\frac{M_{v,Rk}}{\gamma_{M1}}} \leq 1$ $k_{uu} = \frac{C_u}{1 - \frac{N_{Ed}}{N_{cr,Sv,u}}}$ $k_{uv} = C_v$ $k_{vu} = C_u$ $k_{vv} = \frac{C_v}{1 - \frac{N_{Ed}}{N_{cr,v}}}$ <p>$\xi = 1,5$ for SBE members $\xi = 1,1$ for SBU members</p> <p>$N_{cr,Sv,u}$: is the critical axial force for buckling about the major-axis considering the shear stiffness as determined before</p> <p>$N_{cr,Sv,u}$: is the critical axial force for buckling about the minor-axis</p> <p>N_{Rk}: is the characteristic value of the axial force resistance of the built-up section: Af_y</p> <p>$M_{u,Rk}$: is the characteristic value of the major axis bending resistance of the built-up section: $0,9W_{uf_y}$</p> <p>$M_{v,Rk}$: is the characteristic value of the minor axis bending resistance of the built-up section: $0,9W_{vf_y}$</p> <p>C_u, C_v: are the equivalent uniform moment factors determined as follows:</p> $C_u = 0,6 + 0,4\psi_u \geq 0,4 \quad ; \quad -1 \leq \psi_u = \frac{M_{2u}}{M_{1u}} \leq 1$ $C_v = 0,6 + 0,4\psi_v \geq 0,4 \quad ; \quad -1 \leq \psi_v = \frac{M_{2v}}{M_{1v}} \leq 1$ <p>χ_u, χ_v: are the reduction factors for buckling about the major/minor axis</p> <p>χ_{LT}: is the reduction factor for lateral torsional buckling determined based on the critical moment $M_{cr,SV}$ and reduction curve a as follows</p>	<p>prEN1993-1-1 (2019)</p> <p>§8.4.5 Closely spaced-built up members</p>
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		$\bar{\lambda}_{LT} = \sqrt{\frac{0,9W_u f_y}{M_{cr}}}$ $M_{cr} = C_b \pi \frac{\sqrt{E I_v G I_t}}{L}$ <p>I_v: is the second moment of area of the built-up member considered as integral (considering $S_v = \infty$) about its minor axis</p>	
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4 References

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